

**FACIT OCH KOMMENTARER**

- 401 a)**  $11 - x = 22 \Leftrightarrow 11 - 22 = x \Leftrightarrow x = -11$
- b)**  $20x = 12 \Leftrightarrow x = 12/20 \Leftrightarrow x = 0,6$
- c)**  $x/8 = 4 + 4 \Leftrightarrow x = 8 \cdot 8 \Leftrightarrow x = 64$
- d)**  $3x = 4,1 - 3,5 \Leftrightarrow 3x = 0,6 \Leftrightarrow x = 0,6 / 3 \Leftrightarrow x = 0,2$
- 402 a)**  $x/8 = 4 - 3 \Leftrightarrow x/8 = 1 \Leftrightarrow x = 8$
- b)**  $x/0,4 + 1,74 = -0,26 \Leftrightarrow x/0,4 = -0,26 - 1,74 \Leftrightarrow x = 0,4 \cdot -2$   
 $\Leftrightarrow x = -0,8$
- c)**  $x/9 = 18 \Leftrightarrow x = 9 \cdot 18 \Leftrightarrow x = 162$
- d)**  $10x/12 = 8 + 2 \Leftrightarrow 10x = 12 \cdot 10 \Leftrightarrow 10x = 120 \Leftrightarrow x = 120/10$   
 $\Leftrightarrow x = 12$
- 403 a)**  $18 = -8x - 2x \Leftrightarrow 18 = -10x \Leftrightarrow x = -18/10 \Leftrightarrow x = -1,8$
- b)**  $x = 1\ 250/1,25 \Leftrightarrow x = 1\ 000$
- c)**  $6x + 3x = 0 \Leftrightarrow 9x = 0 \Leftrightarrow x = 0/9 \Leftrightarrow x = 0$
- d)**  $-3 - 8 = -4x + 6x \Leftrightarrow -11 = 2x \Leftrightarrow x = -5,5$
- 404 a)**  $3x + 5x = 12 \Leftrightarrow 8x = 12 \Leftrightarrow x = 12/8 \Leftrightarrow x = 1,5$
- b)**  $14 = 3x - x \Leftrightarrow 14 = 2x \Leftrightarrow x = 7$
- c)**  $3 + 5 = 3x + 5x \Leftrightarrow 8 = 8x \Leftrightarrow x = 1$
- d)**  $14 + 10 = -4x + 2x \Leftrightarrow 24 = -2x \Leftrightarrow x = -12$

- 405 a)**  $2x = -22 \Leftrightarrow x = -11$
- b)**  $6x = 20 - 80 \Leftrightarrow 6x = -60 \Leftrightarrow x = -10$
- c)**  $16 - 8 = 0,5x \Leftrightarrow 8 = 0,5x \Leftrightarrow x = 8/0,5 \Leftrightarrow x = 16$
- d)**  $100x = 1,25 + 0,55 \Leftrightarrow 100x = 1,8 \Leftrightarrow x = 0,018$
- 406 a)**  $5x/7 = 15 - 5 \Leftrightarrow 5x/7 = 10 \Leftrightarrow 5x = 70 \Leftrightarrow x = 14$
- b)**  $2x/3 = 14 \Leftrightarrow 2x = 42 \Leftrightarrow x = 21$
- c)**  $0,75x - x = 1,25 \Leftrightarrow -0,25x = 1,25 \Leftrightarrow x = -5$
- d)**  $10 - 25 = -5x + 6x \Leftrightarrow x = -15$
- 407 a)**  $5x + 3 + 2x = x + 21 \Leftrightarrow 7x - x = 21 - 3 \Leftrightarrow 6x = 18 \Leftrightarrow x = 3$
- b)**  $x^2 + 5x + 2x + 10 = x^2 + 3x \Leftrightarrow x^2 - x^2 + 7x - 3x = -10 \Leftrightarrow 4x = -10 \Leftrightarrow x = -2,5$
- c)**  $15x - 3x = 61 - 25 \Leftrightarrow 12x = 36 \Leftrightarrow x = 3$
- d)**  $7x - 5x = 16 + 6 \Leftrightarrow 2x = 22 \Leftrightarrow x = 11$
- 408 a)**  $2x + 2 - 3x + 6 = 4x - 12 \Leftrightarrow -x + 8 = 4x - 12 \Leftrightarrow 8 + 12 = 4x + x \Leftrightarrow 5x = 20 \Leftrightarrow x = 4$
- b)**  $x^2 + x - x - 1 - (x^2 - 2x - 2x + 4) = 2 \Leftrightarrow x^2 - 1 - x^2 + 4x - 4 = 2 \Leftrightarrow 4x - 5 = 2 \Leftrightarrow 4x = 7 \Leftrightarrow x = 1,75$
- c)**  $-2x = x^2 - 2x + 2x - 4 - (x^2 - 2x - 2x + 4) \Leftrightarrow -2x = -4 + 4x - 4 \Leftrightarrow 8 = 4x + 2x \Leftrightarrow 8 = 6x \Leftrightarrow x = 8/6 \Leftrightarrow x = 4/3$
- d)**  $8x + 9 - 6x + 8 = 13x - 4 - 5 + 2x \Leftrightarrow 2x + 17 = 15x - 9 \Leftrightarrow 26 = 13x \Leftrightarrow x = 2$
- 409 a)**  $5x - 2x + 3 = 2 \Leftrightarrow 3x = 2 - 3 \Leftrightarrow 3x = -1 \Leftrightarrow x = -1/3$
- b)**  $9x + 45 - 12 - 8x = 7 - 2x + 2 \Leftrightarrow x + 33 = 9 - 2x \Leftrightarrow x + 2x = 9 - 33 \Leftrightarrow 3x = -24 \Leftrightarrow x = -8$

$$\begin{aligned} \text{c) } & 9(x^2 + x + x + 1) - (6x + 9x^2 - 2 - 3x) = 41 \\ & 9x^2 + 18x + 9 - 6x - 9x^2 + 2 + 3x = 41 \Leftrightarrow 15x + 11 = 41 \Leftrightarrow \\ & 15x = 41 - 11 \Leftrightarrow 15x = 30 \Leftrightarrow \mathbf{x = 2} \end{aligned}$$

$$\begin{aligned} \text{d) } & x^2 - x + 3x - 3 - (x^2 - 3x - 3x + 9) = 2x \\ & x^2 + 2x - 3 - x^2 + 6x - 9 = 2x \Leftrightarrow 8x - 12 = 2x \Leftrightarrow 8x - 2x = 12 \Leftrightarrow \\ & 6x = 12 \Leftrightarrow \mathbf{x = 2} \end{aligned}$$

$$\begin{aligned} \text{410 a) } & \text{Obs: } (6x - 1)/4 = 6x/4 - 1/4 = 1,5x - 0,25 \\ & 3x - 1,5x + 0,25 = 7 \Leftrightarrow 1,5x = 6,75 \Leftrightarrow x = 6,75/1,5 \Leftrightarrow \mathbf{x = 4,5} \end{aligned}$$

$$\text{b) } 2x^2 + 6x + 2x - x^2 - 3x = x^2 \Leftrightarrow 5x = 0 \Leftrightarrow \mathbf{x = 0}$$

$$\begin{aligned} \text{c) } & x^2 + 5x + 2x + 10 = x^2 + 6x + 3x + 18 \Leftrightarrow 7x - 9x = 18 - 10 \Leftrightarrow \\ & -2x = 8 \Leftrightarrow \mathbf{x = -4} \end{aligned}$$

$$\text{d) } 5x - 15 - 3x - 6 - x + 10 = 0 \Leftrightarrow x - 11 = 0 \Leftrightarrow \mathbf{x = 11}$$

**411 a)** 20 % ökning gör att förändringsfaktorn blir **1,20**.

$$\text{b) Ekvation: } \mathbf{1,20 \cdot x = 60}$$

$$\text{c) } 1,20 \cdot x = 60$$

$$\begin{aligned} x &= \frac{60}{1,20} \quad \left[ = \frac{600}{12} = \frac{300}{6} = \frac{150}{3} \right] \\ x &= 50 \end{aligned}$$

Svar: **50 kr**

**412.** Låt den okända sidan i rektangeln ha längden  $x$ . Ekvation:  
 $36 \cdot x = 144$

$$x = \frac{144}{36}$$

$$x = \frac{72}{18}$$

$$x = \frac{36}{9}$$

$$x = \frac{4 \cdot 9}{9}$$

$$x = 4$$

- 413.** Svar: Den andra sidan har längden **4 meter**.  
Låt cirkeln ha radie  $x$  meter. Ekvation ( $\pi \approx 3$ ):

$$3 \cdot x^2 = 300$$

$$x^2 = \frac{300}{3}$$

$$x^2 = 100$$

$$x = \sqrt{100}$$

$$x \approx 10$$

Svar: Cirkelns radie ska vara ca **10 m**.

- 414.** Låt cirkeln ha radie  $x$  meter. Arean för rektangeln är  $10 \cdot 24,3 = 243 \text{ m}^2$ .  
Ekv:

$$\pi \cdot x^2 = 243$$

$$x^2 = \frac{243}{3}$$

$$x^2 = 81$$

$$x = \sqrt{81}$$

$$x = 9$$

Svar: Cirkelns radie ska vara **9 m**.

- 415.** Kvadratens omkrets är  $4 \cdot 12 = 48 \text{ m}$ . Låt cirkeln ha diameter  $x$ . Ekv:

$$\pi \cdot x = 48$$

$$x \approx \frac{48}{3}$$

$$x \approx 16$$

Svar: Radien är ca **8 m**.

- 416.** Antag att bruttolönen är  $x$  kr. 33 % minskning ger en ändringsfaktor på:  
 $1 - 0,33 = 0,67$ . Ekvation:

$$0,67 \cdot x = 16500$$

$$x = \frac{16500}{0,67}$$

$$x \approx \frac{16500}{2/3}$$

0,67 är ungefär  
detsamma som 2/3

$$x \approx 16500 \cdot \frac{3}{2}$$

$$x \approx \frac{49500}{2}$$

$$x \approx 24750$$

Svar: Personen tjänar ungefär **24 750 kr/mån** brutto (mer exakt 24 627 kr).

417. Antag att vi har  $x \text{ m}^3$  under bark. Vi får då ekvationen

$$x \cdot 1,20 = 600$$

$$x = \frac{600}{1,20}$$

$$x = \frac{6000}{12}$$

$$x = \frac{6 \cdot 1000}{2 \cdot 6}$$

$$x = \frac{1000}{2}$$

$$x = 500$$

Svar: Cirka **500 m<sup>3</sup>** under bark.

418. Antag att det hamnar  $x \text{ m}^3$  i A då borde det hamna tre gånger så mycket alltså  $3 \cdot x \text{ m}^3$  i B. Ekvation:

$$x + 3x = 10000$$

$$4x = 10000$$

$$x = \frac{10000}{4}$$

$$x = 2500$$

Svar: Det hamnar ungefär **2 500 m<sup>3</sup> i del A och 7 500 m<sup>3</sup> i del B.**

419. Antag att vi ska tillsätta  $x$  kg vatten. Då blir totalvikten  $2 + x$  kg. Saltvikten är:  $10\%$  av  $2 \text{ kg} = 0,10 \cdot 2 = 0,2 \text{ kg}$ . Dividerar man saltvikten med den totala vikten ska det bli  $5\% = 0,05$ . Ekvation:

$$\begin{aligned}\frac{0,2}{x+2} &= 0,05 \\ 0,2 &= 0,05 \cdot (x+2) \\ 0,2 &= 0,05x + 0,10 \\ 0,2 - 0,1 &= 0,05x \\ 0,1 &= 0,05x \\ \frac{0,1}{0,05} &= x \\ x &= 2\end{aligned}$$

Svar: **2 kg** vatten ska tillsättas.

- 420 a) Pythagoras sats ger:

$$\begin{aligned}15^2 + 10^2 &= x^2 \\ 225 + 100 &= x^2 \\ x^2 &= 325 \\ x &= \sqrt{325} \approx \mathbf{18}\end{aligned}$$



*Här kan man prova sig fram  $17^2 = 289$ ,  $18^2 = 324$ ,  $19^2 = 361$*

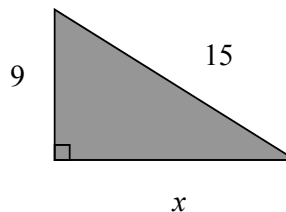
- b) Pythagoras sats ger:

$$\begin{aligned}6^2 + x^2 &= 10^2 \\ 36 + x^2 &= 100 \\ x^2 &= 100 - 36 \\ x^2 &= 64 \\ x &= \sqrt{64} = \mathbf{8}\end{aligned}$$

421. Pythagoras sats ger:  $3^2 + 4^2 = x^2 \Leftrightarrow x^2 = 25 \Leftrightarrow x = \sqrt{25} \Leftrightarrow x = 5 \text{ m}$   
Trädets ursprungliga höjd:  $3 + 5 = \mathbf{8 \text{ m}}$

422. Antagande enligt figur.

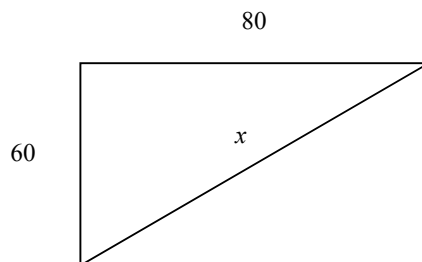
$$\begin{aligned}9^2 + x^2 &= 15^2 \\ 81 + x^2 &= 225 \\ x^2 &= 225 - 81 \\ x &= \sqrt{144} \\ x &= 12\end{aligned}$$



Svar: Den tredje sidan i triangeln är **12 mm**.

423. Antagande enligt figur.

$$\begin{aligned}80^2 + 60^2 &= x^2 \\6\,400 + 3\,600 &= x^2 \\10\,000 &= x^2 \\x &= \sqrt{10000} \\x &\approx 100\end{aligned}$$

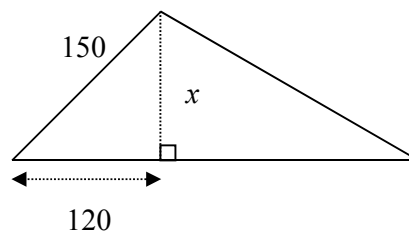


Svar: Diagonalen i rektangeln är ca **100 m**.

424. Antagande enligt figur.
- 
- Beräkna först
- $x$

Ur den vänstra triangeln fås:

$$\begin{aligned}120^2 + x^2 &= 150^2 \\14400 + x^2 &= 22500 \\x^2 &= 22500 - 14400 \\x &= \sqrt{8100} \\x &= 90\end{aligned}$$



$$\text{Arean} = (120 + 180) \cdot 90 / 2 = 300 \cdot 90 / 2 = 27\,000 / 2 = 13\,500 \text{ m}^2 \approx 1,4 \text{ ha}$$

Svar: Områdets area är ca **1,4 ha**.

425 a) 
$$\frac{1}{9x} = \frac{2 \cdot 1}{2 \cdot 9x} = \frac{2}{18x}$$

b) 
$$\frac{7}{6x} = \frac{3 \cdot 7}{3 \cdot 6x} = \frac{21}{18x}$$

c) 
$$\frac{x}{9} = \frac{2x \cdot x}{2x \cdot 9} = \frac{2x^2}{18x}$$

d) 
$$x = \frac{x}{1} = \frac{18x \cdot x}{18x \cdot 1} = \frac{18x^2}{18x}$$

e) 
$$\frac{1}{3} = \frac{6x \cdot 1}{6x \cdot 3} = \frac{6x}{18x}$$

f) 
$$2x^2 = \frac{2x^2}{1} = \frac{18x \cdot 2x^2}{18x \cdot 1} = \frac{36x^3}{18x}$$

426 a) 
$$\frac{2y^2 - y}{y} = \frac{y(2y - 1)}{y} = (2y - 1)$$

b) 
$$\frac{2y - y^2}{y} = \frac{y(2 - y)}{y} = (2 - y)$$

c) 
$$\frac{2xy^2 - y}{y} = \frac{y(2xy - 1)}{y} = (2xy - 1)$$

$$\text{d) } \frac{2y^2 + 3y^3 - y^4}{y} = \frac{y(2y + 3y^2 - y^3)}{y} = (2y + 3y^2 - y^3)$$

$$427 \text{ a) } \frac{(y-2)^2 - 4}{y} = \frac{y^2 - 4y + 4 - 4}{y} = \frac{y(y-4)}{y} = (y-4)$$

$$\text{b) } \frac{(y-3)(y+3) + 9}{y^3} = \frac{y^2 + 3y - 3y - 9 + 9}{y^3} = \frac{y^2}{y^3} = \frac{1}{y} = y^{-1}$$

$$\text{c) } \frac{(y+3)(2y-4) - 2y^2}{y-6} = \frac{2y^2 - 4y + 6y - 12 - 2y^2}{y-6} = \frac{2y-12}{y-6} =$$

$$\frac{2(y-6)}{(y-6)} = 2$$

$$\text{d) } \frac{(1-y)(2y-4) + 2y(y-1)}{4} = \frac{2y-4-2y^2+4y+2y^2-2y}{4} =$$

$$\frac{4y-4}{4} = \frac{4(y-1)}{4} = (y-1)$$

$$428 \text{ a) } \frac{\left(\frac{2}{3} + \frac{1}{2}\right)}{\left(\frac{1}{3} - \frac{1}{6}\right)} = \frac{\frac{6 \cdot 2}{3} + \frac{6 \cdot 1}{2}}{\frac{6 \cdot 1}{3} - \frac{6 \cdot 1}{6}} = \frac{4+3}{2-1} = \frac{7}{1} = 7$$

$$\text{b) } \frac{\left(\frac{3}{y} + 3\right)}{\left(1 + \frac{1}{y}\right)} = \frac{\frac{y \cdot 3}{y} + y \cdot 3}{y \cdot 1 + \frac{y \cdot 1}{y}} = \frac{3+3y}{y+1} = \frac{3(1+y)}{(1+y)} = 3$$



$$\begin{aligned}
 429 \text{ a)} \quad & y = 2x + 3 \\
 & y - 3 = 2x \\
 & \frac{y}{2} - \frac{3}{2} = x \\
 & \frac{1}{2}y - \frac{3}{2} = x \\
 & x = 0,5y - 1,5
 \end{aligned}$$

$$\begin{aligned}
 \text{b)} \quad & 2y - 3x = -5 \\
 & 2y + 5 = 3x \\
 & \frac{2}{3}y + \frac{5}{3} = x \\
 & x = \frac{2}{3}y + \frac{5}{3}
 \end{aligned}$$

$$\begin{aligned}
 \text{c)} \quad & y = \frac{5}{6}x - 1 \\
 & 6 \cdot y = \frac{6 \cdot 5}{6}x - 6 \cdot 1 \\
 & 6y = 5x - 6 \\
 & 6y + 6 = 5x \\
 & \frac{6y}{5} + \frac{6}{5} = x \\
 & x = 1,2y + 1,2
 \end{aligned}$$

$$\begin{aligned}
 \text{d)} \quad & 3y = 2x + 3 \\
 & 3y - 3 = 2x \\
 & \frac{3y}{2} - \frac{3}{2} = x \\
 & x = 1,5y - 1,5
 \end{aligned}$$

$$\begin{aligned}
 430 \text{ a)} \quad & 4y - 3z + 13 = 0 \\
 & 4y + 13 = 3z \\
 & \frac{4}{3}y + \frac{13}{3} = z \\
 & z = \frac{4}{3}y + 4\frac{1}{3}
 \end{aligned}$$

$$\begin{aligned}
 \text{b)} \quad & -3x + 4z - 9 = 0 \\
 & 4z = 3x + 9 \\
 & z = \frac{3}{4}x + \frac{9}{4} \\
 & z = 0,75x + 2,25
 \end{aligned}$$

$$\begin{aligned}
 \text{c)} \quad & 0 = x - 7z - 3 \\
 & 7z = x - 3 \\
 & z = \frac{x - 3}{7} \\
 & z = \frac{1}{7}x - \frac{3}{7}
 \end{aligned}$$

$$\begin{aligned}
 \text{d)} \quad & 5z - y = y + 7z - 3 \\
 & -y - y + 3 = 7z - 5z \\
 & -2y + 3 = 2z \\
 & \frac{-2}{2}y + \frac{3}{2} = z \\
 & z = -y + 1,5 \\
 & z = 1,5 - y
 \end{aligned}$$

431 a)  $\frac{1}{r} = x$   
 $1 = x \cdot r$   
 $\frac{1}{x} = r$   
 $r = \frac{1}{x}$

b)  $\frac{r}{x} + z = 2$   
 $\frac{x \cdot r}{x} + x \cdot z = x \cdot 2$   
 $r + xz = 2x$   
 $r = 2x - xz$   
 $r = x(2 - z)$

c)  $4 = \frac{x}{r} - z$   
 $4r = \frac{r \cdot x}{r} - zr$   
 $4r + zr = x$   
 $r(4 + z) = x$   
 $r = \frac{x}{(4 + z)}$

d)  $5 = \frac{1}{r} - 3$   
 $8 = \frac{1}{r}$   
 $r \cdot 8 = 1$   
 $r = \frac{1}{8}$

432 a)  $a(a - b) = (a + 2)(a - 1)$   
 $a^2 - ab = a^2 - a + 2a - 2$   
 $-ab = a - 2$   
 $2 = a + ab$   
 $2 = a(1 + b)$   
 $\frac{2}{1 + b} = a$   
 $a = \frac{2}{1 + b}$

b)  $0 = 7(ax - 3)$   
 $0 = ax - 3$   
 $3 = ax$   
 $\frac{3}{x} = a$   
 $a = \frac{3}{x}$

c)  $\frac{1}{a} + \frac{2}{a} = \frac{x}{3} + 2$   
 $\frac{3a \cdot 1}{a} + \frac{3a \cdot 2}{a} = \frac{3ax}{3} + 3a \cdot 2$   
 $3 + 6 = ax + 6a$   
 $9 = a(x + 6)$   
 $\frac{9}{(x + 6)} = a$

d)  $\frac{1}{a} - 5x = 4$   
 $\frac{a \cdot 1}{a} - a \cdot 5x = a \cdot 4$   
 $1 - 5ax = 4a$   
 $1 = 4a + 5ax$   
 $1 = a(4 + 5x)$   
 $a = \frac{1}{(4 + 5x)}$

**433 a)**  $s = v \cdot t$

$$\frac{s}{v} = t$$

$$t = \frac{s}{v}$$

**b)**  $d = \frac{m}{V}$

$$V \cdot d = m$$

$$V = \frac{m}{d}$$

**c)**  $v = v_0 + at$

$$v - v_0 = at$$

$$\frac{v - v_0}{t} = a$$

$$a = f^2 kR$$

$$\frac{a}{kR} = f^2$$

$$f = \sqrt{\frac{a}{kR}}$$

**434 a)**  $t = s / v$

**c)**  $a = (v - v_0) / t$

**b)**  $V = m / d$

**d)**  $f = \sqrt{a / (kR)}$